

# Ultrawideband Reflection-Type Metasurface for Generating Integer and Fractional Orbital Angular Momentum

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**Abstract**—Vortex beams carrying orbital angular momentum (OAM) are extensively studied owing to its potential to expand channel capacity of microwave and optical communication. By utilizing the Pancharatnam–Berry phase concept, an ultrawideband single-layer metasurface is proposed to realize the conversion from incident plane waves to reflected vortex beams covering a considerable bandwidth from 6.75 to 21.85 GHz (>105%). An equivalent circuit model combined with broadband phase shift network is developed to effectively design the meta-atoms in metasurface. It is the first time to design wideband metasurfaces with the phase-based characteristics. To verify the proposed model, some deformed square loop meta-atoms are proposed to construct the metasurfaces with broadband OAM characteristic. Moreover, the vortex beams with the integer ( $l = -3$ ), fractional ( $l = -1.5$ ), and high-order ( $l = -10$ ) OAM mode are generated. Based on an OAM spectral analysis, the mode purity of the generated vortex waves is discussed in detail. The experimental results achieve a good agreement with those obtained from the simulation, thus proving the effectiveness and practicability of the proposed method.

**Index Terms**—Fractional orbital angular momentum (OAM) mode, metasurface, OAM, Pancharatnam–Berry (PB) phase, ultrawideband.

## I. INTRODUCTION

SINCE orbital angular momentum (OAM) was known in the optics field in 1992 [1], the vortex waves carrying OAM have gradually become a hot field of research. Like spin angular momentum (SAM), OAM is one of the fundamental physical quantities of electromagnetic (EM) waves. SAM associated with left and right circularly polarized EM waves only offers limited channels. However, OAM can theoretically achieve larger channel capacity by using the orthogonality of different OAM modes [2], [3]. Therefore, different OAM vortex beams have been applied in radio [4]–[6], optical [3], [7], fiber [8], [9], and quantum communications [10] to

achieve high spectral efficiency and communication capacity. However, the issues of misalignment, doughnut-shaped pattern, and mode crosstalk in OAM systems still deserve a further study. Some excellent analytical methods have been proposed to understand the limitations of those radiating systems [11]–[13]. Moreover, some useful applications of OAM were also reported including super-resolution imaging [14]–[16], structure field formation [17], [18], optical tweezers [19], and astronomy [20].

It is well known that OAM vortex beams, characterized by doughnut-shaped field, have helical phase front with the azimuthal phase term of  $e^{jl\varphi}$  (where  $l$  is the topological charge, and  $\varphi$  is the azimuthal angle around the propagation axis). Therefore, it is a basic principle to generate vortex beams with the OAM mode  $l$  by introducing a constant electric current with a consecutive phase of  $l\varphi$  along a circle. One common way is to introduce the desired phase retardation by using spiral phase plates [21], [22] and holographic plates [23]. Obviously, this phase retardation relies on the light propagation over distances much larger than the wavelength to shape the wavefronts, which is difficult, if not totally impossible, to construct ultrathin components. The circular antenna array [24]–[26] is another approximated way to produce OAM vortex waves with discrete currents based on Nyquist's theory. However, it requires a complex feeding network. By exploiting the Pancharatnam–Berry (PB) phase concept [27], one can produce abrupt changes in phase, amplitude, or polarization of EM waves based on the ultrathin components, which is so-called “metasurface.” Resonant metasurfaces are composed of resonant scattering units (V-shaped [28], [29] and square loop shaped [30]) with varied geometric parameters and can generate linearly polarized OAM waves. Unfortunately, controlling abrupt phase through geometric parameters is hard to achieve broadband and high performance. Several kinds of metasurfaces have been designed to deal with the problem based on the spin-to-orbital conversion (PB phase) theory [31]–[40]. In microwave regime, a perfect electric conductor (PEC)–perfect magnetic conductor (PMC) metasurface was demonstrated to achieve nearly 100% conversion efficiency within a narrow bandwidth [39]. A four-layer metasurface was also proposed to achieve 33% bandwidth and approximate 60% efficiency [35]. However, those previous works mentioned still suffer from narrow bandwidth, low efficiency, and

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bulky structure. Recently, the ultrathin reflection-type metasurfaces were proposed such as the dual-layer metasurfaces with spatially rotated parallel dipoles [41] and the single-layer metasurfaces with spatially rotated double arrow-shaped meta-atom [42]. Although they can generate the vortex beams with a considerable wide bandwidth, they still lack a reliable model to design these meta-atom structures.

In this article, an equivalent circuit (EC) model combined with broadband phase shift network is proposed to design those meta-atom structures. On one hand, the EC model based on lumped element provides a physical insight on the broadband EM behavior of those meta-atom structures. On the other hand, this constructed EC model can be utilized to choose appropriate structures and parameters for meta-atoms rather than time-consuming and aimless numerical simulation. In particular, some effective EC models for deformed square loops are demonstrated. The corresponding reflection-type metasurfaces composed of the rotated deformed square loop meta-atoms are further designed to convert the circularly polarized EM beams with SAM into EM vortex waves with both SAM and OAM within an ultrawide frequency range. The generated integer, fractional, and high-order vortex beams are decomposed and discussed in detail. The simulated and experimental results verify the proposed metasurfaces.

## II. DESIGN THEORY OF PROPOSED METHOD

### A. Spin-to-Orbital Conversion

It is convenient to adopt a Jones formalism to analyze the incident and scattered fields for an anisotropic meta-atom in metasurface [43], [44]. The reflected and incident fields can be connected by the reflection coefficients in reflected Jones matrix, and the SAM-to-OAM process can be demonstrated as [39]

$$r_{ll} = 0.5[(r_{xx} - r_{yy}) + j(r_{xy} + r_{yx})]e^{-2jk\varphi} \quad (1a)$$

$$r_{lr} = 0.5[(r_{xx} + r_{yy}) + j(r_{yx} - r_{xy})] \quad (1b)$$

$$r_{rl} = 0.5[(r_{xx} + r_{yy}) - j(r_{yx} - r_{xy})] \quad (1c)$$

$$r_{rr} = 0.5[(r_{xx} - r_{yy}) - j(r_{xy} + r_{yx})]e^{2jk\varphi} \quad (1d)$$

where  $r_{xx}$ ,  $r_{yy}$ ,  $r_{ll}$ , and  $r_{rr}$  are the copolarized reflection coefficients under  $x$ -,  $y$ -, left circularly, and right circularly polarized normal incidence. Also,  $r_{xy}$ ,  $r_{yx}$ ,  $r_{lr}$ , and  $r_{rl}$  are the corresponding cross-polarized reflection coefficients. From (1a) and (1d), an abrupt phase change  $e^{-j2k\varphi}$  ( $e^{j2k\varphi}$ ) could be introduced by a meta-atom with a rotating angle of  $k\varphi$ . A helical phase wavefront could also be obtained by a metasurface composed of rotated meta-atoms. Therefore, the first task is to design a meta-atom with high copolarized reflection coefficients  $r_{rr}$  and  $r_{ll}$ . If a meta-atom is mirror symmetric with respect to the  $yz$  plane or  $xz$  plane as shown in Fig. 1(b), the corresponding  $r_{xy}$  and  $r_{yx}$  in Jones matrix satisfy  $r_{xy} = r_{yx} = 0$  [44]. To generate a high SAM-to-OAM conversion within a wide bandwidth, the  $r_{xx}(\omega)$  and  $r_{yy}(\omega)$  of meta-atom should satisfy following conditions [45]:

$$|r_{xx}(\omega)| \approx |r_{yy}(\omega)| \approx 1 \quad (2)$$

$$\arg(r_{xx}(\omega)) - \arg(r_{yy}(\omega)) \approx \pm\pi. \quad (3)$$

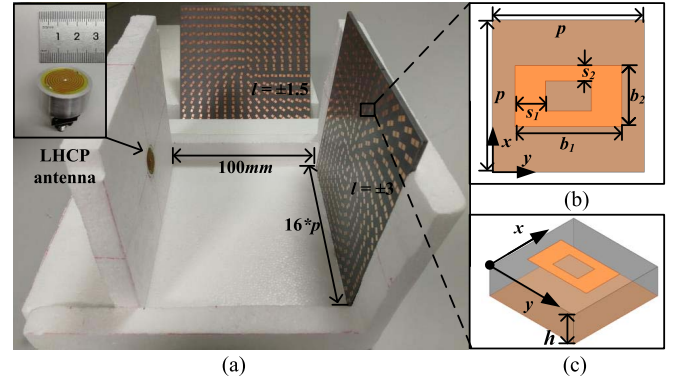


Fig. 1. (a) Photograph of vortex-beam-generating device. (b) Top view of the meta-atom. (c) Side view of the meta-atom.

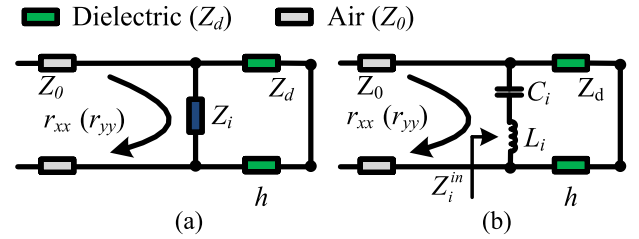


Fig. 2. (a) Equivalent transmission-line model of the single-layer metasurface meta-atom. (b) Specific lumped parameter equivalent electrical circuit models of proposed deformed square loop metasurface.

### B. EC Analysis

As shown in Fig. 1, a single-layer dielectric substrate (F4B,  $\epsilon_r = 2.65$ ,  $h = 3$  mm) is considered in this article to maintain simple and ultrathin features, which is the same as that employed in [42]. Fig. 2(a) illustrates the corresponding EC model, where  $Z_0 = 377 \Omega$  is the wave impedance of air.  $Z_d = Z_0/(\epsilon_r)^{0.5} = 231.6 \Omega$ , the wave impedance of equivalent transmission line, is related to the dielectric substrate. The length ( $h = 3$  mm) of the equivalent transmission line corresponds to the thickness of the dielectric layer. The metal ground is modeled as a short circuit.  $Z_i$  ( $i \in \{1, 2\}$ ), the equivalent impedances in  $x$  and  $y$  polarization incident fields, respectively, depend on the specific periodic metal structure printed on the dielectric. Some valid equivalent lumped circuit models of  $Z_i$  have already been built for some common periodic meta-atom structures in the literature [46]–[49], such as the mesh of metal strips (equivalent inductance), the array of metal patch (equivalent capacitance), and the array of square loop (a series LC circuit). According to the wideband model of reflection-type phase-shifter [50], a series-connected LC network is important to make its reflection coefficient ( $r_{xx}$ ,  $r_{yy}$ ) easier to satisfy (3) within a wide frequency range. Therefore, the array of square loops is a promising candidate to generate wideband vortex beams. Without the dielectric and metal loss, their modulus of reflection coefficients  $|r_{xx}|$  and  $|r_{yy}|$  in Fig. 2 are invariably equal to one and a high reflectance in (2) can be achieved within the considered frequency range. In order to produce the  $180^\circ$  phase difference in (3), a deformed square loop meta-atom structure is proposed in Fig. 1(b) and (c), and its equivalent electric circuit is shown in Fig. 2(b).

Reflection coefficients  $r_{xx}$  and  $r_{yy}$  of corresponding circuits can be written as

$$r_{xx} = |r_{xx}|e^{j\phi_x} = \frac{Z_i^{in} - Z_0}{Z_i^{in} + Z_0}, \quad (i = 1) \quad (4a)$$

$$r_{yy} = |r_{yy}|e^{j\phi_y} = \frac{Z_i^{in} - Z_0}{Z_i^{in} + Z_0}, \quad (i = 2) \quad (4b)$$

where

$$Z_i^{in} = \frac{jZ_d \tan(\beta h) * \left(j\omega L_i + \frac{1}{j\omega C_i}\right)}{jZ_d \tan(\beta h) + j\omega L_i + \frac{1}{j\omega C_i}}. \quad (5)$$

In (4) and (5),  $Z_{i=1}^{in}$  and  $Z_{i=2}^{in}$  are the impedances of the ECs under corresponding  $x$  and  $y$  polarized incident.  $\beta$  is the propagation constant in the dielectric slab.  $\phi_x$  and  $\phi_y$  are phases of the  $x$  and  $y$  polarized reflection coefficients, respectively. The phase difference  $\phi$  is defined as follows:

$$\phi = \phi_x - \phi_y. \quad (6)$$

To obtain a wideband phase difference  $\phi \approx \pi$ ,  $\phi$  has to satisfy the following condition for the frequencies ranging from  $\omega_1$  to  $\omega_2$ :

$$\frac{d\phi}{d\omega} \approx 0, \quad \text{for all } \omega \in (\omega_1, \omega_2) \quad (7a)$$

$$\phi(\omega_1) = \phi(\omega_2) = \pi. \quad (7b)$$

Substituting (4)–(6) into (7), one can derive a set of effective capacitance and inductance values ( $L_1 = 4.51$  nH,  $L_2 = 5.09$  nH,  $C_1 = 0.014$  pF,  $C_2 = 0.040$  pF) for a frequency range from 9 to 20 GHz. The corresponding results of the EC model are shown in Fig. 3. Within the operating bandwidth, the phase difference  $\phi$  remains to be  $180^\circ \pm 40^\circ$  and the  $d\phi/df$  remains to be  $\pm 15^\circ/\text{GHz}$ , which verifies that such a model can achieve a broadband  $180^\circ$  phase difference between  $x$  and  $y$  polarization reflection coefficients. Since no obvious resonance occurs in the operating bandwidth, the reflection phases  $\phi_x$  and  $\phi_y$  maintain a small change, which is also the key point for the proposed meta-atom to achieve the wideband and high-efficiency characteristics.

Combined with the empirical formula and the resonating nature of the square loop [47], [49], the desired values of capacitance and inductance could be obtained by adjusting the geometric parameters of the deformed square loop. As the value of  $b_1$  changes, this mainly affects the coupling capacitance  $C_2$  between adjacent cells along the  $y$ -direction, which eventually affects the  $y$ -direction reflection phase  $\phi_y$  as shown in Fig. 3(a). Similarly, the changes in the value of  $s_2$  mainly affects the inductance  $L_2$ , which eventually influences on the  $y$ -direction reflection phase  $\phi_y$  as shown in Fig. 3(b). Correspondingly, the reflection phase  $\phi_x$  can be controlled by changing the values of  $s_1$  and  $b_2$ . By adjusting the geometric parameters of the deformed square loop, the reflection phase of meta-atom obtained from the simulation is consistent with those from the proposed EC model.

Moreover, the geometric parameter of  $b_1$  mainly affects the low-frequency part of reflection phase  $\phi_y$  as shown in Fig. 3(a), which determines the low-frequency cutoff frequency ( $\omega_1$ ) and low-frequency passband performance of

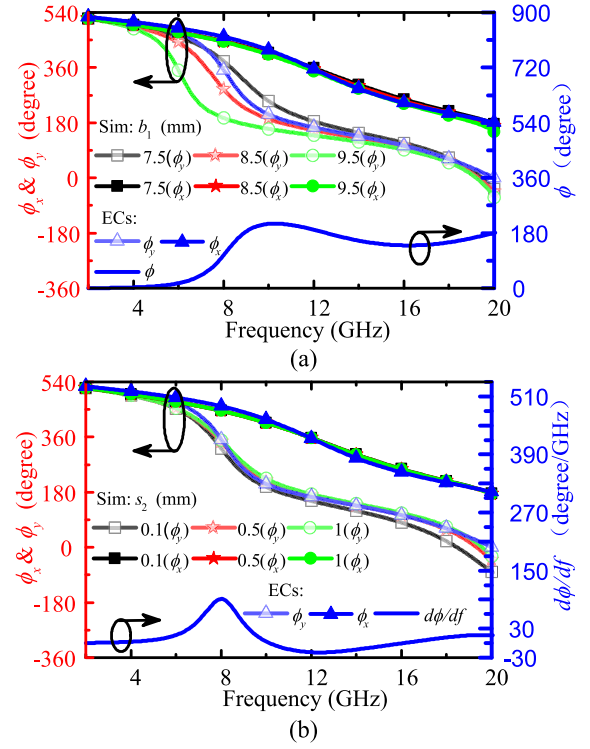


Fig. 3. Simulation (Sim) and equivalent circuits (ECs) models are calculated. Simulation results of  $\phi_x$  and  $\phi_y$  as a function of (a)  $b_2$  and (b)  $s_2$ . Other parameters are (a)  $b_2 = 3$  mm,  $s_1 = 3.5$  mm,  $s_2 = 0.5$  mm, and  $p = 10$  mm and (b)  $b_1 = 8$  mm,  $b_2 = 3$  mm,  $s_1 = 3.5$  mm, and  $p = 10$  mm.

the meta-atom. The geometric parameter of  $s_2$  mainly affects the high-frequency part of reflection phase  $\phi_y$  as shown in Fig. 3(b), which affects the high-frequency passband performance of the meta-atom. Correspondingly, the geometric parameter of  $b_2$  also affects the low-frequency passband performance of the meta-atom. The geometric parameter of  $s_1$  determines the high-frequency cutoff frequency ( $\omega_2$ ) and high-frequency passband performance of the meta-atom. These guidelines will be utilized in the design of the proposed meta-atoms.

### III. SIMULATION AND EXPERIMENTAL RESULTS

#### A. Simulation Results of Unit

According to the equivalent model of the proposed meta-atom and the optimization guidelines in Section II-B, two meta-atoms are designed to achieve the expected bandwidth by adjusting the parameters  $b_1$  and  $s_2$  of the meta-atom in Fig. 3. One is for ultrawideband ( $r$ ) and the other is for high-performance ( $r'$ ). The design parameters of ultrawideband meta-atom are  $p = 10$  mm,  $b_1 = 9.2$  mm,  $s_1 = 3.5$  mm,  $b_2 = 3$  mm,  $s_2 = 1.1$  mm, and  $h = 3$  mm. The design parameters of high-performance broadband meta-atom are  $p = 10$  mm,  $b_1 = 8$  mm,  $s_1 = 3.5$  mm,  $b_2 = 3$  mm,  $s_2 = 0.3$  mm, and  $h = 3$  mm. Their numerical simulation results can be obtained by a commercial software HFSS. As shown in Fig. 4(a), both the reflection coefficients at  $x$ -polarization and  $y$ -polarization are close to one with a nearly  $\pi$  phase difference within a wide frequency bandwidth, which is crucial for an ultrawideband OAM beam generation. The working



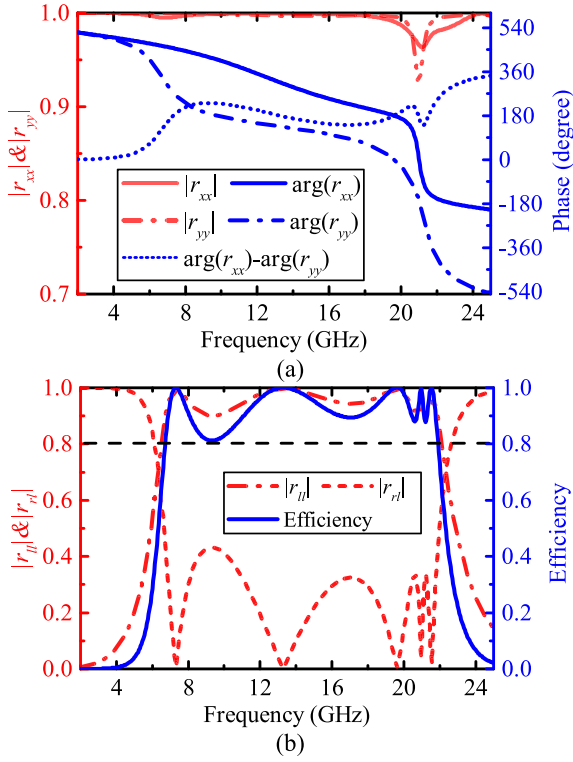


Fig. 4. Reflection spectrum for an ultrawideband (105%) meta-atom ( $r$ ) under (a) LP and (b) CP excitations. In (b), the corresponding efficiency is also included.

efficiency ( $efficiency = 2|(r_{xx} - r_{yy})/2|^2 / (|r_{xx}|^2 + |r_{xy}|^2 + |r_{yx}|^2 + |r_{yy}|^2)$ ) is calculated to measure the conversion performance as illustrated in Fig. 4(b). The proposed ultrawideband meta-atom keeps co-polarization reflection  $r_{ll}$  higher than 0.9 and efficiency higher than 0.81 within a wide bandwidth ranging from 6.75 to 21.85 GHz. The achieved 105.6% fractional bandwidth is significantly higher than the existing 82% fractional bandwidth of the multimode metasurface [41] under the same efficiency condition. In order to avoid the obvious resonance frequency around 21 GHz (which also exists in the mentioned multimode metasurface), another high-performance broadband meta-atom is designed by adjusting the parameters  $b_1$  and  $s_2$ . A major phase change of  $r_{yy}$  is introduced which leads to the phase difference between the  $x$ -polarization ( $r'_{xx}$ ) and the  $y$ -polarization ( $r'_{yy}$ ) reflection coefficients more close to  $\pi$  within 8.55–19.95 GHz as shown in Fig. 5(a). As a result, a higher co-polarization reflection ( $r'_{ll} \geq 0.96$ ) and higher efficiency (efficiency  $\geq 0.9$ ) can be obtained as depicted in Fig. 5(b). It is important to observe from Fig. 5(c) that the phase responses are paralleled as expected and that the co-polarization reflection coefficients are all higher than 0.95 within the expected frequency band for different rotation angles, both of which are essential for the constructed metasurface with high-purity OAM characteristic. In addition, the proposed broadband meta-atom achieves a fractional bandwidth of 80%, which is significantly higher than the existing fractional bandwidth of 40% (12–18 GHz) in high-performance double-arrow-shaped metasurface [42].

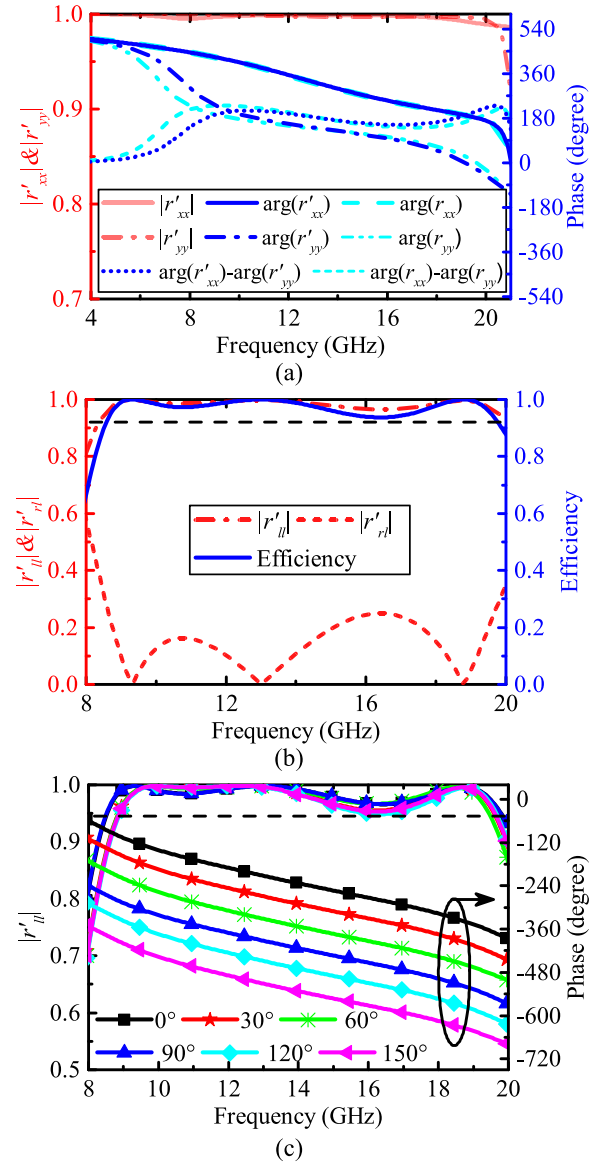


Fig. 5. Reflection spectrum for a high-performance broadband meta-atom ( $r'$ ) under (a) LP and (b) CP wave excitations. In (a), the results of ultrawideband meta-atom ( $r$ ) are included. In (b), the corresponding efficiency is also included. (c) Reflection spectrum for the high-performance broadband meta-atom with different rotation angles under CP wave excitations.

### B. Numerical Near-Field Results of Metasurface

As the spin-to-orbital conversion concept discussed above, a metasurface with a desired vortex phase profile  $e^{jl\varphi}$  can be constructed by arranging the mentioned meta-atoms at different  $\varphi$  with a certain rotated angle  $k\varphi$ . Here,  $\varphi$  is the azimuthal angle around the vortex beam, and  $l = 2k$  is the OAM mode (topological charge) of the generated vortex beams. As shown in Fig. 6, the specific topologies of metasurfaces with  $l = \pm 1, \pm 1.5, \pm 2$ , and  $\pm 3$  are composed of a  $16 \times 16$  array of the rotated meta-atoms. To illustrate the wideband behavior of the proposed metasurfaces, both the near-field and far-field EM performances have been demonstrated to verify its vortex property. Under the excitation of a left-handed (LH) circular polarization plane wave, the vortex beams with the OAM mode of  $l = -1.5$  and  $l = -3$  are generated separately by the

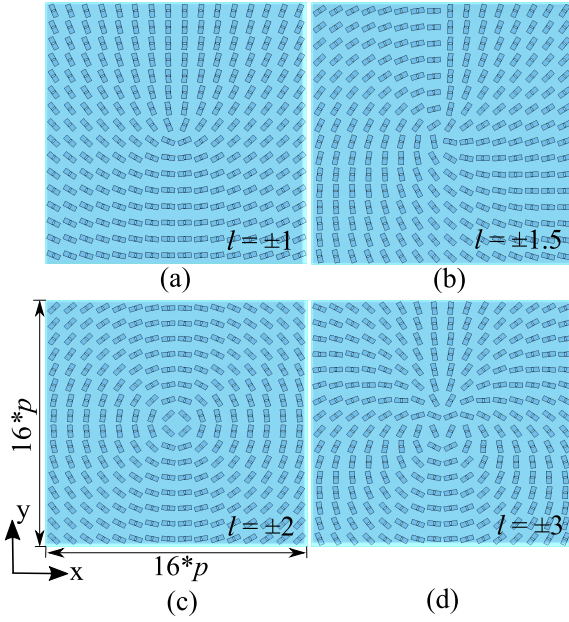


Fig. 6. Layouts of the proposed metasurface with the OAM mode of (a)  $l = \pm 1$ , (b)  $l = \pm 1.5$ , (c)  $l = \pm 2$ , and (d)  $l = \pm 3$ .

proposed metasurfaces in this article. At different frequencies, both the LH and right-handed (RH) components of reflected electric field are sampled and decomposed in Figs. 7 and 8. The sampling plane size is  $180 \text{ mm} \times 180 \text{ mm}$  and the distance between the metasurface and sampling plane is  $100 \text{ mm}$ . A donut-like amplitude and vortex phase of electric field can be found from the LH component in the sampling field, which are consistent with the OAM wave characteristics. For a quantitative analysis of the purity of the OAM modes, the Fourier transform analysis is implemented to decompose the individual OAM modes. The corresponding equations are given as follows [51]:

$$A_l = \frac{1}{2\pi} \int_0^{2\pi} \psi(\varphi) e^{-jl\varphi} d\varphi \quad (8)$$

$$\psi(\varphi) = \sum_l A_l e^{jl\varphi} \quad (9)$$

where  $\psi(\varphi)$  is a function of the sampled field along the circumference of the  $z$ -axis, where the LH component electric field peaks in the sampling plane. Here, the OAM modes from  $l = -5$  to  $l = 5$  are considered and the energy weight of the OAM mode  $l$  is defined as follows:

$$\text{energy weight} = \frac{A_l}{\sum_{l'=-5}^5 A_{l'}}. \quad (10)$$

The Fourier analysis results in Fig. 7 shows that the expected OAM mode  $l = -3$  is the main part in the LH (co-polarized) component of the reflected electric field and other OAM modes in the LH component are small enough to be ignored except for some possible interference OAM modes  $l = -3 \pm 4n$  ( $n \in \mathbb{Z}$ ) which are introduced by the directional anisotropy of square lattice. For the RH (cross-polarized) component of the reflected electric field, the OAM mode  $l = 0$  occupies the dominant part. The energy weight of RH component primarily depends on the efficiency of the spin-to-orbital conversion of the proposed meta-atom. As shown

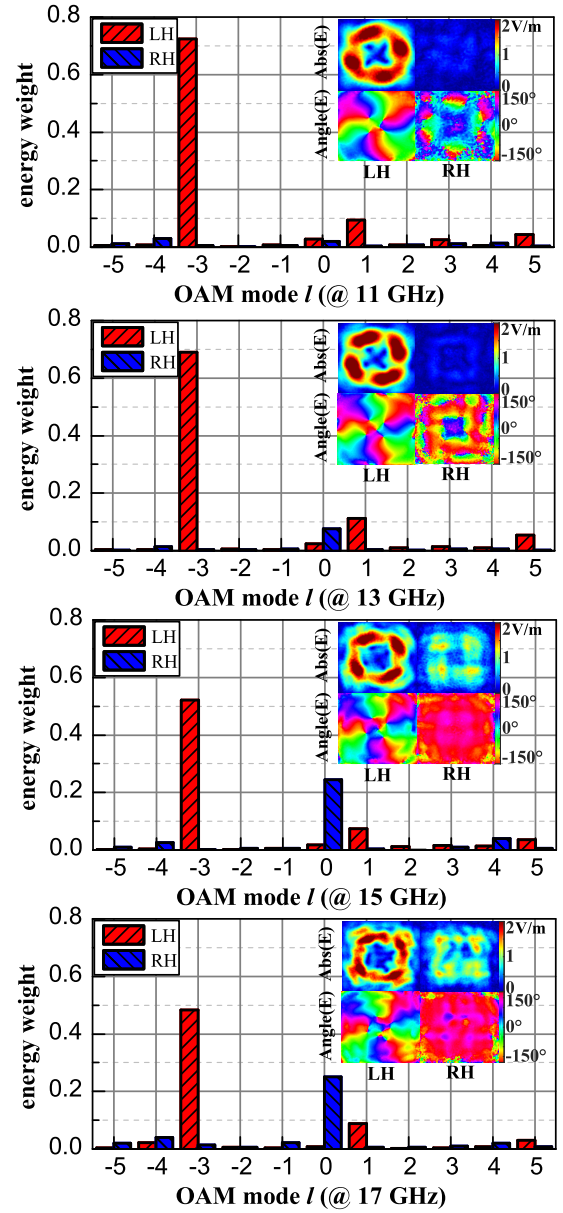


Fig. 7. Near-field observation and corresponding spectral analyses of the generated  $l = -3$  vortex beams at different frequency. The sampling plane size is  $180 \text{ mm} \times 180 \text{ mm}$  and the distance between the metasurface and sampling plane is  $100 \text{ mm}$ .

in Fig. 5(b), since a higher conversion efficiency can be obtained in frequency range from 9 to  $14 \text{ GHz}$  than frequency range from  $14$  to  $18 \text{ GHz}$ , the generated  $l = -3$  vortex beams possess a higher energy weight at  $11$  and  $13 \text{ GHz}$  (around  $70\%$ ) than that at  $15$  and  $17 \text{ GHz}$  (around  $50\%$ ).

Fig. 8 shows a Fourier spectrum analysis of the generated  $l = -1.5$  vortex wave, where  $l$  in (8) satisfies  $l = -1.5 \pm n$  ( $n \in \mathbb{Z}$ ) to maintain the orthogonality of the fractional OAM mode for LH component. Similar results can be obtained in the same way as the generated  $l = -3$  vortex wave. One significant difference between the fractional modes and the integer ones is that the amplitude zeros (phase singularities) of the fractional modes occur not only in the center but also spread out in one direction ( $+y$  direction in this article). It results in a notched

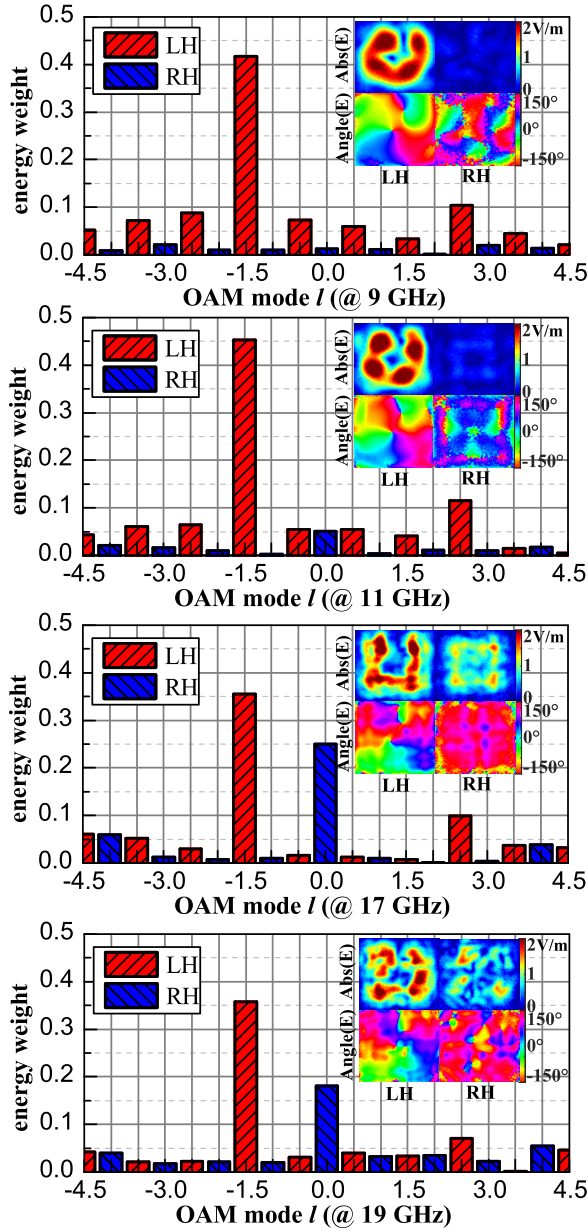


Fig. 8. Near-field observation and corresponding spectral analyses of the generated  $l = -1.5$  vortex beams at different frequency. The sampling plane size is  $180 \text{ mm} \times 180 \text{ mm}$  and the distance between the metasurface and sampling plane is  $100 \text{ mm}$ .

donut-shaped radiation pattern as shown in Fig. 8. In addition, such a phase-singularity structure also causes a fact that the purity of the fractional mode (0.35–0.45 energy weight) is lower than the integer mode (0.48–0.75 energy weight).

### C. Numerical and Experimental Far-Field Results of Metasurface

The corresponding Fourier spectral analysis is further implemented for the generated far-field OAM vortex beams.  $\theta$  and  $\varphi$  are the polar and azimuthal angles in the spherical coordinates, respectively. The sampling polar angle  $\theta$  is taken at the maximum point in electric field pattern. For the far-field spectral analysis of the generated  $l = -1.5$  vortex beam

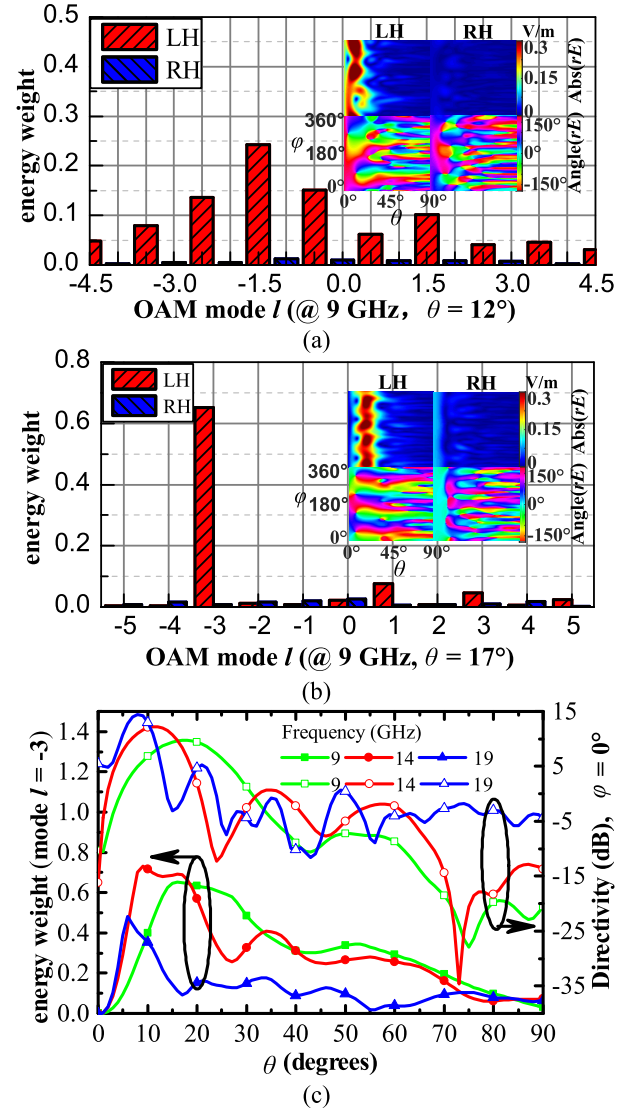


Fig. 9. Spectral analyses of the generated far-field vortex beams with the OAM mode. (a)  $l = -1.5$ . (b)  $l = -3$ . (c) Both far-field directivity and energy weight of the generated vortex beam with the OAM mode  $l = -3$  at different sampling polar angle  $\theta$ .

in Fig. 9(a), the mode  $l = -1.5$  still occupies the most energy weight. However, the energy weight at far-field is obviously attenuated in comparison with the near-field results. Note that the energy of  $l = -1.5$  mode at far-field is converted into adjacent fractional modes. The notched doughnut patterns become unobvious than that of the near-field results, which implies that the fractional order modes are not suitable for long-distance transmission. For the generated far-field beams with the OAM mode  $l = -3$ , a uniform amplitude and a continuous phase of far-field electric field are obtained at a polar angle  $\theta = 17^\circ$  in Fig. 9(b). Consequently, a high-purity vortex spectrum with the energy weight of 0.65 can be obtained by (10). It means that the proposed metasurface can produce high-purity integer-order vortex waves at both the near- and far-fields. By observing the directivity of generated vortex beams in Fig. 9(c), the main lobe of the pattern becomes narrower and the number of side lobes increases as



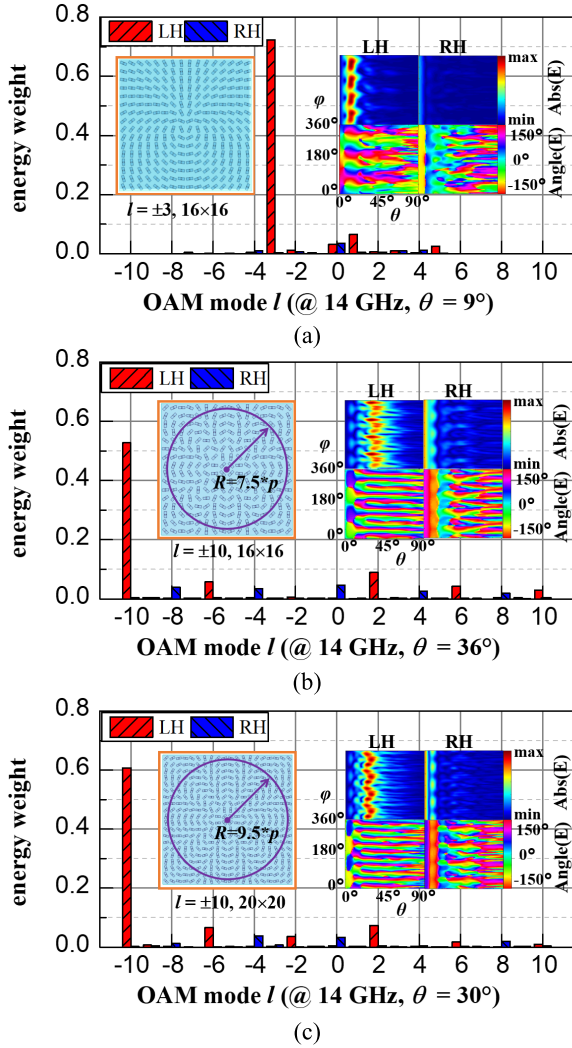


Fig. 10. Far-field spectral analyses of vortex beams generated by metasurfaces with (a)  $l = \pm 3$ ,  $16 \times 16$  array, (b)  $l = \pm 10$ ,  $16 \times 16$  array, and (c)  $l = \pm 10$ ,  $20 \times 20$  array. The corresponding LH and RH components of far-field electric field are also included.

the frequency increases, which have the same characteristics as the vortex beams generated by the antenna array [2]. As shown in the corresponding energy weight in Fig. 9(c), the mode purity near the main lobe reaches its highest value, which is crucial for the reception of high-performance vortex waves.

A high-order vortex beam with the OAM mode  $l = -10$  is generated by the metasurface with a  $16 \times 16$  array of the proposed meta-atoms. Its corresponding far-field spectral analyses from  $l = -10$  to  $l = 10$  are also shown in Fig. 10(b). Compared with the results generated by  $l = -3$  metasurface in Fig. 10(a), the higher order vortex beam suffer more from its divergence angle and uneven amplitude of the main lobe. Therefore, a wider spectral crosstalk and a lower energy weight 0.53 could be achieved. In principle, it can be understood as the Nyquist sampling theorem that the metasurface also needs a certain number of meta-atoms to approximately produce vortex waves with high-order OAM. Based on the results in Fig. 10(a) and (b), it is reasonable to observe

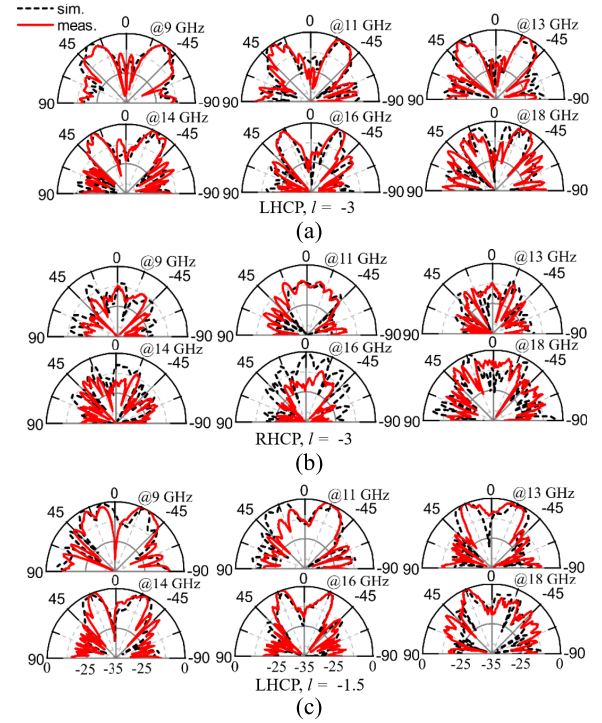


Fig. 11. Comparisons of the simulated and measured normalized patterns in the  $xoz$  plane under the excitation of an LHCP spiral antenna. (a) Co-polarized LHCP and (b) cross-polarized RHCP patterns of the proposed metasurface with  $l = -3$ . (c) LHCP patterns of the proposed metasurface with  $l = -1.5$ .

that the vortex waves with the high-order modes are not as robust (high performance) as when  $l$  is small under the same size and structure of metasurface. Fig. 10(c) shows a larger  $l = \pm 10$  metasurface with a  $20 \times 20$  array of meta-atoms and corresponding spectral analyses. The amplitude of generated vortex beam shows a more uniform distribution along  $\varphi$  than the case of metasurface with a  $16 \times 16$  array of meta-atoms. The corresponding spectral analyses prove that increasing the effective area of metasurface ( $R^2$ ) or the effective number of meta-atoms can improve the energy weight of the generated vortex wave (from 0.53 to 0.61 in this case), which is the key point to produce the high-order and high-purity vortex waves by the metasurface. Moreover, the divergence angle of the main lobe is also reduced from  $\theta = 36^\circ$  to  $\theta = 30^\circ$  by increasing the area ( $R^2$ ) of metasurface, as shown in Fig. 10(b) and (c).

For the experimental verification, both the metasurfaces with  $l = \pm 3$  and  $l = \pm 1.5$  are fabricated and measured. A wideband LH Archimedes spiral antenna with  $\text{VSWR} \leq 2$  and an axial ratio less than 4 dB within 7–18 GHz is used for the excitation. Moreover, the spiral antenna can benefit from its small cross-sectional radius of 12 mm to ensure negligible influence on the reflected vortex beams. The transmitting antenna and metasurface are fixed on a foam box at a distance of 100 mm as shown in Fig. 1(a). Both the measured and simulated patterns are normalized to the co-polarized (LHCP) pattern. As shown in Fig. 11, the measured patterns of the modes  $l = -3$  and  $l = -1.5$  are consistent with the

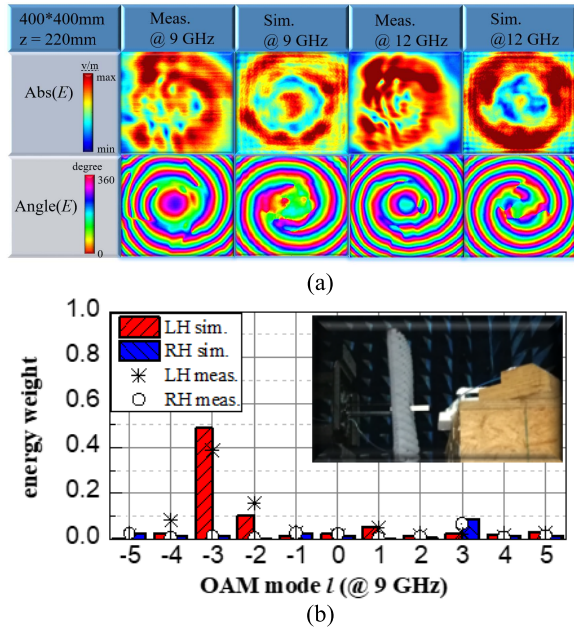


Fig. 12. Near-field sampling results under the excitation of an LHCP spiral antenna. (a) Amplitude and phase distributions of reflection vortex beam with the OAM mode  $l = -3$ . (b) Spectral analyses of the sampling results. The photograph of corresponding experimental system is also included.

simulated patterns varied from 9 to 18 GHz. The cross-polarization (RHCP) patterns of  $l = -3$  are significantly lower than the co-polarization (LHCP) patterns, except for the high-frequency patterns at 16 and 18 GHz, where the conversion efficiency of metasurface is small. The hollow patterns suggest that both the  $l = -3$  and  $l = -1.5$  reflection beams carry the OAM characteristics. One difference is that the patterns of the  $l = -1.5$  vortex wave become less of symmetric in comparison with the  $l = -3$  case.

#### D. Numerical and Experimental Near-Field Results of Metasurface

The sampling plane size is 400 mm  $\times$  400 mm and the distance between the metasurface and the sampling plane is 220 mm. The spiral antenna is placed between the metasurface and the sampling plane to excite the circularly polarized plane waves for the metasurface with OAM  $l = \pm 3$ . Hollow vortex beams can effectively avoid the excitation antenna placed on the z-axis. The results of the low-frequency parts are shown in Fig. 12(a). The amplitude and phase distributions of measurement reflection vortex beam are good agreement with the simulation results. The expected null appears in the central region of the electric field magnitude and the phase front of the generated vortex beam winds by  $6\pi$  around the z-axis, which are the typical vortex wave characteristics with the OAM mode  $l = -3$ . The OAM spectra of the sampling results are shown in Fig. 12(b). The energy weight of the expected OAM mode  $l = -3$  occupies the dominant part (nearly 39–49% energy weight) which verifies the proposed metasurface with the OAM mode  $l = \pm 3$ . Notice that the achieved performance is also determined by the excitation antenna and the alignment of the sampling plane.

#### IV. CONCLUSION

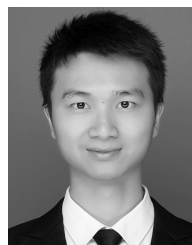
In this article, a single-layer broadband meta-atom has been proposed based on the deformed square loop structure. With such a meta-atom, a simple and high-performance metasurface has been synthesized to generate OAM vortex beams within a wideband range from 8.55 to 19.95 GHz. Moreover, the corresponding EC model has been established and the proposed broadband meta-atom can be analyzed and designed effectively. The proposed meta-atoms can be further applied to other phase-based devices due to its high efficiency and broadband features, and this broadband model can also be extended to the transmission structures. Moreover, the vortex beams with the fractional and high-order OAM modes have also been generated and analyzed, which may find further applications in target detection and communication systems. The OAM spectral analyses of both near-field and far-field have been performed, which illustrates the high-purity vortex characteristics of the proposed metasurface more intuitively.

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